REIRIEVING ISHE NEORMATION RESERVOIRS a WORKSTATION ENVIRONMENT RETRIEVING TEXT FROM SMALL TO LARGE

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#### ABSTRACT

Commercially available database management systems provide access to data as their main forte. P-trees facilitate access to numerical data as their main namerical data; for example, free text information composed of a mixture of numerical and bibliographic data. This kind of processing mixture of mancrical and sistic graphic data. This wind or processing<br>requires significant string manipulation which is not available in commercial database products which operate on small workstations connected to larger hosts.

tree data structures of type P, sometimes called the PATRICIA type This paper describes a near optimal method of storing, searching and retrieving derived frcm the "trie" structure; particularly the use of The method is very efficient and is suitable for use on small<br>workstations as very efficient and is suitable for use on small workstations as well as large computer systems. The development and applications of the paged P-tree method are described along with appropriate performance comparisons. The database applications software, based on P-trees, for providing small workstation users access and manipulation capabilities within a large information<br>repository.composed.of.tour.capabilities within a large information y composed of textual and numerical data, is reviewed.

#### INTRODUCTION

The class of indexing methods based on the Fredkin "trie"<br>''S have been liness f structure have been known for many years. Fredkin (1960). The term "trie" is derived from letters imbedded in the word "retrieval". This data structure can be used to represent sets of character strings and/or abstract data types. Consequently, it is an extremely versatile data structure. An algorithm based on the binary trie structure was developed in the in the mid sixties, Morrison (1967, 1968). The method is called Practical Algorithm To Retrieve Information Coded in Alphanumeric" or PATRICIA for brevity. The tree described by PATRICIA is called a P-tree or a tree of type PATRICIA, CLARK (1973), Lagana et al (1980).

Trie structures are closely associated with a number system. The binatural B number system, B is a natural extension of the counting or Cardinal number system, Morrison (1972). B is characterised by a first member 1, and a pair of successors functions, L for left and R for right successors. B has many representations which differ not only in form but also in use. Binary P-trees are a special case of the free monoid <sup>i</sup> with two generators. on the set {0, 1}, which can be formed from the Binatural number system, and plays an essential role in the coding of information for binary digital computers.

facilitate the indexing, modifying, querying and retrieving of information in a binary coded data base. The data structure is especially suitable for dealing with variable length keys, and/or similar titles, and/or similar textual phrases stored within a large file, Clark (1972), Knuth (1973). The selection of a proper alphabet on which P-trees should operate need not be restricted to binary. M-ary be alphabets could be used; however the allocation of storage and efficiency of inner loops are made easier if the alphabet is binary, Clark (1972). In addition the vast majority of computers manipulate P-trees and store information in a binary manner.

An is example where text an important paramater appears in enabling scientific notebooks to become machine readable. Many other examples having a commercial as well as scientific orientation are<br>examples having a commercial as well assemenced of numerical and frequently encountered. Text bibliographic data provides unique <sup>&</sup>lt; frequently encountered. Text when composed lengths.<br>hibitary chief data provides unique and difficult challenges. when composed of numerical and

are commercially available data. not even those based on manipulate ivailable database management systems <sup>&</sup>lt; Very few commercially availance and most even those based the relational model, Pollard et al (1984).

era. small of free text technological for use on is left to packages such as IBM's Products of this ilk are workstations and even The manipulation STAIRS, from the 1973 genera11y precluded minicomputers.

A few authors briefly mention the area of text searches. Almost all available DBMS implementations and text books assume the Almost all available DBMS implementations and text-books assume the<br>database is "formatted" and is highly-structured. Most information database is formatted and is magicy - and the textual databases, retrieval appricutions are allowed the commercial databases involving e.g. Sciencitic wasservest in the banking industry. Adhoc queries against these kinds of database are very complex, Date (1983).

P-trees are an <mark>excellent mechanism for providing free text</mark> manipulation not only on large computers but also on small workstations.

## P-TREES OF TYPE PATRICIA-1

rithm recognises those bit locations which are<br>important in distinguishing love Ough hits are one way branches. This is done by including in each node the number of bits to skip over before making the next branch test, Knuth (1973).<br>The contents of a P-tree indox are making the next branch test, Knuth (1973). The contents of a P-tree index are pointers to locations within a data<br>base target, and pointers to enable by a locations within a data wase target, and pointers to enable branching decisions. The method examines the bit pattern of the specified encoding, e.g. ASCII or<br>EBCDIC. The algorithm recognizes is encoding, e.g. ASCII or determined determined to be<br>called "twin bits" twin bits". Important in distinguishing keys. Such bits are The PATRICIA algorithm forms an N-node binary search tree based on the binary representation of keys, without storing keys in the nodes. In particular, the index which a P~tree defines includes no keys or text, only numbers weys of text, only numbers which point to other P-tree nodes or storage locations of keyed targets in the data base. The fundamental periodic state of the fundamental in the data base. The fundamental in the state of the fundamental in the data base. The fundamental in the state of the fundame behind P-trees is to build a Fredkin like binary trie by avoiding<br>one-way branches. This is done by includi algorithm re of a and

the string of bits, tion of key **x** 1.e. a string of 0 s and 1 s, which <sup>is</sup><br>key K. Then K has described as Then K has two daughters <sup>or</sup> <sup>Consider</sup> a st encoded representati.

permutations which are extensions of K; namely KO and Kl, (K with "O"<br>... "I'" concriented) or "I" concatenated). If both KO and KI are keys, then K is a branch key and KO and KI are twin keys. If only one of KO and KI is a key then K is not a branch key. Keys are in the same chain of keys if they have right extensions in common; hence are possible keys in one or more data base records. On a search if a key is not found, the algorithm at least locates those keys which have the most initial bits in common. (1972). Clark Figure 1. For a pro forma of P-trees of type PATRICIA-I, see

In all cases data base target records are retrieved in collating In fact the algorithm can be applied to problems sequence order. In fact the algorithm " *<sup>c</sup>* encountered in sorting and is particularly useful when sorting records involving long variable length keys in very long records, Cooke (1985).

forward and economical in computation time, Clark (1972), Lagana As mentioned above, the index, i.e. the P-tree nodes consist When keys are presented to the system the computation time required to determine the presence or absence of an cwner record is bounded, the bound depending linearly on the length-of-the-key-and being independent of the size of the data base—and—the—number—of occurrences. (1980). only of numbers; hence the keys appear in their proper place, in their natural form in the data base. The data base is also unrestricted in format, special The algorithms for updating the data base are straight Items in the data base donotneed to be arranged in any New additions do not necessitate relocating or shuffling information around in the data base. Keys and data-base order. targets need not be in one-to-one correspondence since one data base target may be <sup>&</sup>gt; retrievable by as many keys as have been connected to it. One key *<sup>r</sup>* may retrieve as many targets in the data base as it has occurrences.

#### P-TREES OF TYPE PATRICIA-II

Computer implementation of the original\_algorithm, PATRICIA-I, of computer memory constraints in that the P-tree core the size of data bases rescricted the size of data modulated quantity of memory was required<br>operational environment. A substantial quantity of data. At that time the method to large volumes of data. At that time when applying the method to large volumes of random access<br>computers were not equipped with large quantities of random access were not equippose<br>In fact, PATRICIA-I could efficiently handle a data base with memory. In fact, PATRICIA-1 could efficiently random memory words<br>approximately R/5 keys, R being the number of random memory words resident, Clark (1972). This limitation hases which could be indexed as well as the was limited because had to be entirely restricted computers approximately R/5 keys,



## Figure 1.

Pro forma of an in-core PATRICIA-I P-tree, ti-represents the twin Pro forma of an in-core PATRICIA-I P-tree. ti represents<br>bits. A branch path from ti to ti represents a chain of kovs oranch path from ti to tj represents a chain of keys.

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and out of memory as required; hence at most one page of the upper and overlaid P-tree index, which significantly reduced this storage limitation, Clark (1972). PATRICIA-II was implemented on several large e.g. CDC 6600 and 7600 and used extensively on very large computers, <sup>&</sup>lt; data bases at the Los Alamos National Laboratory. PATRICIA-II was designed to build a lower index, which is always core resident, and an upper index, divided into pages which are stored on disk. Each upper index page references only itself and the data base. Both the and the upper index are P-trees. Second level P-trees are swapped in available, Morrison (1968). At the time R/5 was of the order of a few thousand, index, along with the lower index is core resident at any given time. Performing a transaction, i.e. an insertion, deletion or search, normally requires <sup>&</sup>lt; one disk access to fetch required pages of the upper level index into memory.

#### P-TREES OF TYPE PATRICIA-III

P-tree however, the system was designed and implemented for an interactive PATRICIA-III was implemented on the DEC System 10 and UNIVAC 1100 series on-line systems and is still in use in a-parts-data-base environment, extended on-line environment. Thompson (1975). two-level This implementation essentially uses the algorithms developed for PATRICIA-II;

n-levels, thus removing the constraint of two-level indexing. In PATRICIA-II and III, at some point in time, a given second level page index could become full and a new second level page must be spawned. In essence this means the full page must be split, forming a dead part and a live part. The spawned page being the complement of its parent, i.e. dead nodes in the spawned page are live nodes in the parent page and vice versa. When the second level page-spawning-occurred, a Recently the two-level P-tree structure has been-extended-to pointer to the new page had to be added to the lower index, ultimately increasing the size of the core resident lower page. This approach yields P-tree structures which are "low in height", which may induce second level pages, Clark (1972), Korbin (1983). PATRICIA-II and many second level pages, Clark (1972), Korbin are constrained by having the lower page memory resident as well For a pro forma of P-trees of type PATRICIA-II and III, see Figure 2. III as nonsplitable.



# Figure 2.

Pro forma P-tree representation of P-trees of type PATRICIA-II and<br>PATRICIA-III.

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### P-TREES OF TYPE PATRICIA-IV

inherent efficiency of the original algorithm. The method can now be applied without any of the original constraints on the number of keys, P-tree to grow in a more normal manner. That is the lower P-tree, or root <sup>j</sup> page, can also be split and spawn a new level of pages, along with a new root page. The original algorithm has now been fully extended, and implemented in PATRICIA-IV while at the same time retaining the In PATRICIA-IV, the algorithm has been enhanced to enable the or the host machine resources.

one or two mass <sup>1</sup> storage accesses(s) to fetch the final page for Using multilevel indexing, each transaction normally results in referencing the <sup>&</sup>lt; data base. In practice, this number increases very slowly with the size of the data base. In fact, increasing the number of keys by three upper level PATRICIA-I algorithm, the number of disk accesses is bounded above by the number of key occurrences in the data base for search and delete transactions. For insertion, the number of disk accesses is bounded by the number of key occurrences in the data being added to the data base,Clark (1972), Korbin (1983). orders of magnitude increases the average number of page faults by one, Clark (1985, unpublished). As in the

structure, Morrison (1983). This multiple purpose data structure is called a MAP, an acronym for matching and permutation. A MAP is a The only tabulation required to describe a map is the function. The only primitive structure change after P-trees, or trees of type PATRICIA, exist in several similar data structures. algorithm, requires that the index rake use of a multiple purpose data Finite set in which each member, x, has a spouse and a successor. The spouse function is a matching and the successor function is a permutation. The<br>successor function. successor initialisation accomodating hosts to several data structures including binary trees. To extend the two level P-tree, used in the PATRICIA-II initialisation is a successor swap. MAPS are efficient and

memory and the time for updating and transmission by a similar factor. This is a werkstation n-level paged P-trees is similar to a pure binary tree. The only differences are that as well as each node having zero or two children, each tree node also has a spouse. Nodes are divided into two sets, In a typical application, the use of a MAP host reduces the requirement for describing a data structure by a third to half, significant reduction; especially when viewed in a small environment. The MAP specifically used in extending to workstation environment. The MAP specifically used in extending to

internal node's right child is to be the successor of the matching. record the successor of each node. This extended P-tree data structure record the successor of each node: This complete tree by successively exchanging the successors of two nodes. internal nodes called women and external nodes called men. An internal nodes called women and external nodes carrow mere the internal mode s right dirit is defined by the left child is defined Korbin (1983), MOTITSON (1999). The spouse relationship is a marriage or matching. In essence the MAP need only

The importance of the MAP data structure is realised when one considers the operations of adding or deleting material from the data base. New internal as well as external tree nodes must be created or released during the transactions of adding and deleting. In addition, mass storage released by the deletion of data base material must also be freed for potential reuse at a later date. These two types of transactions require that the algorithm be able to create as well as free for later use P-tree nodes and physical mass storage locations.

In practice, the only portion of the n-level P-tree which is (lowest level page), and every limb, (a higher level page), has a swapped into memory when required. Limbs reference themselves or higher level limbs or the data base, Korbin (1983). For a pro forma of r-trees of type PATRICIA-IV, see Figure 3. memory resident is the P-tree root, (also called the ''trunk"), and at most one other page, (called a limb), of the upper index. The trunk, positive integer associated with it called the limb number. Limbs are

## SUMMARY AND FUTURE DIRECTIONS

near optimal and performance is Empirical results show that the P-tree algorithm for searching is<br>Optimal and performance expectations, near optimal and performance is consistent with theoretical<br>expectations, Clark (1972), Knuth (1973), Lagana (1980), Korbin (1985, through PATRICIA-IV, it must be published). For PATRICIA-I through PATRICIA-IV, it must be noted that the method applies to any<br>set of keys in any data base that the method applies to any set of keys in any data base. Retrieval computational effort is independent of the order in which material is added to the data base.<br>The binary search, e.g. applies only to an ouder added to the data base. and Clark the order in which material

In general, trie trav<br>inserting, deleting and  $\epsilon$ <br>time proportional to the<br>(1983). to the length of which can be performed in In general, trie traversal is quite efficient. The operations of time proportional to the length of the word involved, Aho et al



Figure 3.

Pro forma of P-trees of type PATRICIA-IV.



a p-tree balancing algorithm has been developed which is much like B-tree balancing. It requires only linear time, on the average, for balancing and keeps search time bounded. (search time)<1.5\* (search time for a perfectly balanced tree).

Empirical Empirical results using variable length keys show that the P-tree algorithm yields better performance than B+ trees and/or hashing approaches. In addition, P-trees are particularly useful when implementing spelling dictionary/checkers on small systems.

At present PATRICIA-IV is implemented on the DEC VAX in PASCAL, <sup>C</sup> and FORTRAN running under VMS and/or UNIX. <sup>A</sup> joint Singapore and Australian development project is presently being carried out by implementing the n-level P-tree algorithm on a network of IBM type PC's linked to a network of VAX systems. The system provides small workstation users access to large volumes of unstructured information composed of textual as well as numerical data. The distributed data base resides on the VAX's mass storage devices. The n-level P-tree index resides on individual PC's where users perform transactions. This approach off-loads the data base transactions and frees the main system for other users. When actual references to the distributed VAX data base are determined on the PC workstation, then the contents of the physical data base locations are returned to the PC user. The task of searching through an index, most of which resides on mass storage, is performed in the PC. Multiple on-line users of the same data base index must compete for computer resources and index access.

of small micro or personal seeking access to the data base index-and/or-the-data-base itself.<br>Individual PC users can baye that index-and/or-the-data-base-itself. users providing Many computer systems do not provide enough raw power and system to adequately cope with several terminals simultaneously<br>ccess to the data base in terminals simultaneously information storage and retrieval filtraction of particular interest<br>mormation storage and retrieval filtributed PC users local personal <sup>&</sup>lt; involving Individual PC users can have their own customised index which is down<br>line loaded, providing access to me customised index which is down ine loaded, providing access to information of particular interest<br>held on the central data base, which is information of particular interest facilities far beyond the <sup>A</sup> similar approach could be used features seeking capabilities of personal computers, <sup>i</sup> in a situation involving a networking computers.

providing a form of distribute practical and economical d data base capabilities to show that this J a form <sup>Results</sup> show that this method is a ve means of users. of distributed

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